Stage 6 Knowledge Organiser (Corbett Maths video numbers in brackets)

1. Identify common factors of two or more numbers (219)
2. Identify common multiples of two or more numbers (218)
3. Fully simplify a given fraction (146)
4. Adding and subtracting fractions with different denominators (133)
5. Solve one step algebraic equations (110)
6. Find a fraction of an amount (137)
7. Find a percentage of an amount $(234,235)$
8. Find the missing term in a sequence (287)
9. Calculate the area of rectangles, triangles and parallelograms ( $45,44,49$ )
10. Calculate the volume of cubes and cuboids (355)
11. Solve a recipe problem (256)
12. Draw an enlargement (no centre) (104)
13. Use a two-step formula
14. Use a protractor to draw and measure angles $(<180)(28,31)$
15. Angles in triangles and quadrilaterals $(33,37)$
16. Construct a pie chart (163)
17. Round to powers of 10 (277a, 277b)
18. Calculate the mean of a list of numbers (53)
19. Plot coordinates in all 4 quadrants (84)
20. Translate a shape by a worded vector (325)

| Skill | Method | Keywords/Definitions |
| :---: | :---: | :---: |
| 601 | Identifying Common Factors <br> List the factors of both number and find any factors that appear in both lists <br> Example: Find the common factors of 12 and 20 <br> So, the common factors of 12 and 20 are 1,2 and 4 | Factors of a number can divide equally into that number. Common factors are factors of one or more numbers. |
| 602 | Identifying Common Multiples <br> List the multiples of each number and find ones that appear in both lists <br> Example: Find a common multiple of 6 and 9 <br> Multiples of 6 include: $6,12,18,24,30$ <br> Multiples of 9 include: $9,18,27,36,45$ <br> So, 18 is a common multiple of both 6 and 9 | Multiples of a number are found by multiplying that number by a whole number (their times tables) |
| 603 | Fully Simplify a Given Fraction <br> Divide both the numerator and denominator by the same thing until you cannot find any more numbers that both can be divided by. <br> Example: Simplify $\frac{36}{42}$ <br> 2 is a factor of both 36 and 42 so we can divide both numbers by 2 which gives us $\frac{18}{21}$ <br> 3 is a factor of both 18 and 21 so we can divide both numbers by 3 which gives $\frac{6}{7}$ <br> There are no more common factors so $\frac{6}{7}$ is simplified fully. | Equivalent fraction: where the same fraction can be show using different numbers than the ones given |
| 604 | Adding, Subtracting, Multiplying and Dividing Fractions <br> For adding and subtracting use equivalent fractions to get both fractions to have the same denominator then add/subtract numerators. <br> Example: Calculate $\frac{6}{7}-\frac{3}{5}$ <br> Multiply the $\frac{6}{7}$ by $\frac{5}{5}$ and the $\frac{3}{5}$ by $\frac{7}{7}$ which gives $\frac{30}{35}-\frac{21}{35}$ (this is known as cross multiplication) <br> Now the denominators are equal we can subtract numerators to give $\frac{9}{35}$ <br> Use the exact same method for an addition, just add the numerators at the end instead of subtracting them. <br> For multiplying fractions multiply the numerators together and multiply the denominators together. <br> Example: Calculate $\frac{2}{7} \times \frac{3}{8}=\frac{6}{56}$ which simplifies to $\frac{3}{28}$ | Numerator- top number Denominator-bottom number Equivalent fractionthe same fraction written with different numbers |


|  | For dividing fractions flip the second fraction only upside down and multiply this fraction by the first fraction. Example: Calculate $\frac{3}{4} \div \frac{5}{6}$ turn the second fraction upside down and multiply the three quarters by this new fraction $\frac{3}{4} \times \frac{6}{5}=\frac{18}{20}$ then this simplifies to $\frac{9}{10}$ |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 605 | Solve one step algebraic equations <br> Use the inverse operation $t$ find the value of the letter, remembering that whatever you do to one side of an equation you must do to the other to keep it balanced. <br> Example: solve <br> $x-7=12 \quad$ Get rid of the -7 here by using the inverse operation: +7 on both sides <br> $+7 \quad+7$ this 'deletes' the -7 on the left hand side but adds 7 onto the 12 on the right hand side $x=12$ <br> Remember that terms like $5 x$ mean ' 5 multiplied by $x$ ', and. $\frac{x}{6}$ means ' $x$ divided by 6' |  |  |  |  |  |  |  |  |  | Equations have letters numbers AND an equals sign. Inverse means opposite: so add and subtract are inverse and multiply and divide are inverse. |
| 606 | Find a Fraction of an Amount: <br> Draw a diagram to represent the fraction you want to find. Use the amount given to find what's in each block, then count up the blocks you have shaded. <br> Example: Find $\frac{3}{7}$ of $£ 210$ <br> this diagram represents the $\frac{3}{7}$ as 3 out of the 7 blocks are shaded. <br> so if the whole diagram represents the $£ 210$, we can divide the $£ 210$ into the 7 blocks and count up the blocks we shaded: $£ 30+£ 30+£ 30=£ 90$ <br> So, $\frac{3}{7}$ of $£ 210$ is $£ 90$ |  |  |  |  |  |  |  |  |  |  |
| 607 | Finding a Percentage of an Amount: <br> Find $10 \%$ (and $5 \%$ if needed) then use these to find the percentage you want. <br> Example: Find $35 \%$ of 80 g <br> Each block here represents $10 \%=8 \mathrm{~g}$ and from this we can find the $5 \%=4 \mathrm{~g}$ |  |  |  |  |  |  |  |  |  | Percent means 'out of 100 ' <br> To find $10 \%$ divide by 10 |


|  | $\begin{gathered} 10 \%=8 \mathrm{~g} \\ 10 \%=8 \mathrm{~g} \\ 10 \%=8 \mathrm{~g} \\ +5 \%=4 \mathrm{~g} \\ \hline 35 \%=28 \mathrm{~g} \\ \text { So } 35 \% \text { of } 80 \mathrm{~g}=28 \mathrm{~g} \\ \hline \end{gathered}$ |  |
| :---: | :---: | :---: |
| 608 | Finding a missing term in a sequence <br> Decide what the rule is for the sequence then use this to find the missing term. <br> Example: Find the next term in the following sequence 38131823 <br> The rule here must be +5 so the next term is $23+5=28$ | A sequence is a pattern of numbers following a rule |
| 609 | Finding the area of rectangles, parallelograms and triangles. <br> For a rectangle and parallelogram area $=$ length x width <br> Area $=12 \mathrm{~cm} \times 2 \mathrm{~cm}=24 \mathrm{~cm}^{2}$ <br> Area $=9 \mathrm{~cm} \times 5 \mathrm{~cm}=45 \mathrm{~cm}^{2}$ Note that the 6 cm is <br> NOT the height <br> For a triangle area $=$ base x height $\div 2$ (a triangle is effectively a rectangle cut in half) <br> Area $=5 \mathrm{~cm} \times 12 \mathrm{~cm} \div 2=30 \mathrm{~cm}^{2}$ again note that the 12 cm is the height here, NOT the 13 cm | Height must be straight up in shapes, not slanty! Units for area should always be squared $\mathrm{m}^{2} \mathrm{~cm}^{2} \mathrm{~mm}^{2}$ etc |
| 610 | Finding the volume of cubes and cuboids <br> Multiply the length, width and height together (these will all be the same for a cube) Example: Find the volume of the following cuboid | Length, width and height can be replaced with different names for example base, height, depth etc Units here should all be cubed to show it is a 3 D space $\mathrm{cm}^{3} \mathrm{~m}^{3}$ etc |


|  | Volume $=4 \mathrm{~cm} \times 20 \mathrm{~cm} \times 25 \mathrm{~cm}=2000 \mathrm{~cm}^{3}$ |  |
| :---: | :---: | :---: |
| 611 | Solve a Recipe Problem <br> Recipes work using direct proportion (if one thing doubles, everything else needs to double etc) <br> Example: Below are the measurements to make 8 scones. How much of each ingredient would be needed to make 20 scones? <br> 8 Scones <br> 200g flour <br> 30 g caster sugar <br> 50 g butter <br> 140 ml milk <br> 1 egg <br> IF we double everything here we get 16 scones, if we treble ( $x 3$ ) we get 24 , so we cant just do that but $16+4=20$ so find the measurements for 16 and the measurements for 4 and add these to get the measurements for 20 . |  |
| 612 | Draw an Enlargement <br> Us the scale factor of enlargement to decide how bog each of the new, enlarged sides of the shape needs to be. | Scale factor - what each side length |

## Example: On the grid draw an enlargement of the triangle using scale factor 3



As we have a scale factor of 3 , the base wil go from being 4 units across to 12 units across


To enlarge the right hand diagonal side we need to count squares. It goes 1 square left and 2 squares up, so when it is enlarged it will need to go 3 squares left and 6 squares up


As this gives us the top point on the triangle we can join it up to the base to
complete the enlargement.
613 Use a Two Step Worded Formula
A formula is a set of instructions to do to an 'input' number that will give you a corresponding 'output' number.
A two-step formula has two operations to do to the input to find the output.
Example: To convert between degrees Celcius and degrees Farneheit you can use the basic formula:

$$
\text { Temperature in Farenheit }=\text { Temperature in Degrees } \times 2+32
$$

Calculate the Farenheit temperature when it is $24^{\circ}$ Celcius
If we know that the 'temperature in degrees' is 24 then we can put that into our formula:

$$
\text { Temperature in Farenheit }=24 \times 2+32
$$

Using BIDMAS to calculate this gives us $48+32=80^{\circ} \mathrm{F}$
We can also be given the 'output' and asked to find the 'input'
Example: Using the same temperature formula above, if the temperature is given as $92^{\circ}$ Farenheit, what is the temperature in degrees celcius?
This time replace the 'temperature in Farenheit' with 92 to give

$$
92=\text { Temperature in Degrees } \times 2+32
$$

So we now need to solve this using inverse operations. So we subtract 32 and then divide by two (remember to do the opposite order to BIDMAS when using inverse operations)
$92-32=60 \div 2=30^{\circ} \mathrm{C}$

A Formula is a set of instructions to get from an input to an output.
They can also be algebraic, and you know some formulae already like:
Area=Length $x$ Width
Degrees Celcius and Degress Farenheit are two measures of temperature. In the UK we normally use Celcius.

| 614 | Using a Protractor to Measure and Draw Angles <br> Measuring an Angle: <br> Its always a good idea to decide if your angle is acute or obtuse before measuring so you can see if your answer makes sense. <br> For example in the diagrams above, would an answer of $58^{\circ}$ make sense? <br> Check that you have drawn the right type of angle once drawn (acute or obtuse) | A protractor is a semi-circular piece of equipment we use to measure and draw angles. <br> Acute angle - less than 90 <br> Obtuse angle = between 90 and 180 |
| :---: | :---: | :---: |
| 615 | Use the Angle Facts Angles in Triangles and Angles in Quadrilaterals <br> Rule: Angles in triangles always add up to $180^{\circ}$ <br> Rule: Angles in quadrilaterals always add up to $360^{\circ}$ <br> Example: find angle $x$ <br> Add up the angles that we know: | Quadrilateral - a shape with 4 sides. There are lots of different types of quadrilaterals that we come across in maths. |

$75+80=155$

$$
70+50+90=210
$$

remember the little box means $90^{\circ}$
So to find the missing one, subtract this from the total we know from the rule
$180-155=25$

$$
360-210=150
$$

## 616 Construct a Pie Chart

Example: construct a pie chart from the frequency table below

| Colour | Frequency |
| :---: | :---: |
| Blue | 25 |
| Green | 14 |
| Red | 21 |

Add up your frequencies to find the total
$25+14+21=60$
What we now need to decide is what number links our total frequency (60) to the total for the degrees in a pie chart (this is
ALWAYS 360 as a pie chart is always in the shape of a circle)
So we divide $360 \div 60=6$
This means to find the angle we need to draw for each colour we must multiply the frequency by 6 each time

| Colour | Frequency |
| :---: | :---: |
| Blue | 25 |
| Green | 14 |
| Red | 21 |
| $6=6=8450$ |  |

Draw on the angles to your circle accurately using a protractor, making sure to move around the circle after you've drawn each one so you don't overlap the sections.


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617 Round to the Nearest 10, 100 and 1000
Rounding a number means giving it as the closest 10,100 or 1000. To decide which one it is closest to, decide the two it lies
in between then use the rule " }5\mathrm{ or more go up, otherwise go down"
Examples:
Round 47 to the nearest }1
47 lies between 40 and 50. As it is over 45 we round up to 50
Round 729 to the nearest 100.
729 lies between 700 and 800. As we are rounding to the nearest 100, it is the digit in the tens column that we look at to
decide whether to go up or down. The tens has a 2 in it this time so we round down to 700
Round 12503 to the nearest 1000
In terms of 1000, we 503 lies between 12000 and 13000 . As we are rounding to 1000 it will be the hundreds column that we look at to decide whether to round up or down. This time the hundreds has a 5 in it so we round up to 13000
Calculate the Mean of a List of Numbers
The mean is a type of average. An average is a typical or normal value for a group.
mean \(=\frac{\text { total }}{\text { count }} \quad\) Where the total is the numbers added up and the count is how many numbers there are.
Example: Find the mean of the following numbers \(13,6,10,6,4,8,17,9\)
Total \(=13+6+10+6+4+8+17+9=73\) the count here is 8 as there are 8 numbers
So, mean \(=\frac{73}{8}=9.125\)
619 Plot Coordinates in all 4 Quadrants
A coordinate is made up of two numbers in a bracket, separated by a comma. They show us a specific place on a grid of numbers. The first number lines up with the \(x\) axis (going across) and the second numbers lines up on the \(y\) axis (going up and down.
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